

# Transport coefficients in the pre-equilibrium stage

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Exploring Quark-Gluon Plasma through soft and hard probes,  
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# Outline

- ▶ Bottom-up thermalization,
- ▶ QCD kinetic theory
- ▶ Jet momentum broadening  $\hat{q}$
- ▶ Heavy quark diffusion  $\kappa$

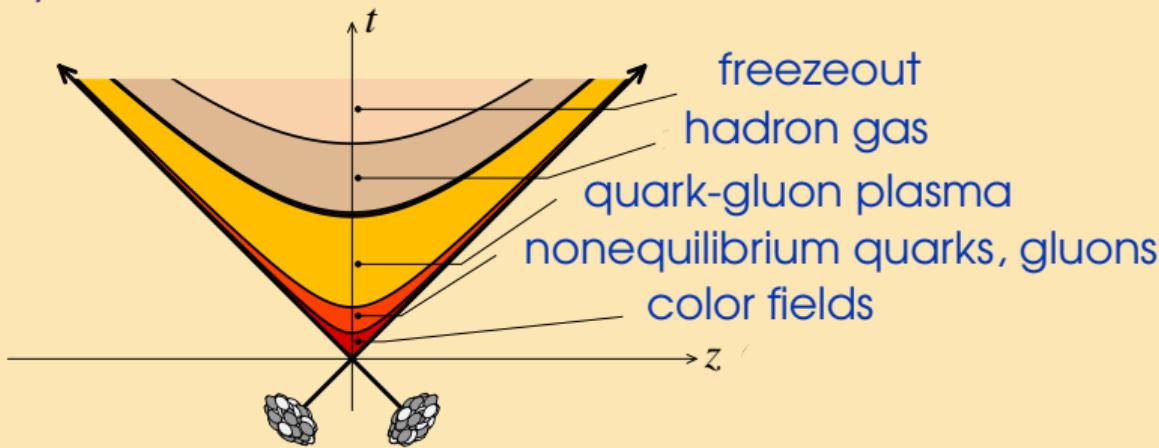
This talk:

- ▶ Heavy quark diffusion coefficient in heavy-ion collisions via kinetic theory,  
K. Boguslavski, A. Kurkela, T. L., F. Lindenbauer, J. Peuron, [arXiv:2303.12520 \[hep-ph\]](#)
- ▶ Jet momentum broadening during initial stages in heavy-ion collisions,  
K. Boguslavski, A. Kurkela, T.L., F. Lindenbauer, J. Peuron, [arXiv:2303.12595 \[hep-ph\]](#)
- ▶ 1+1D boost invariant expansion

Goal: calculate transport coefficients  $\hat{q}$  and  $\kappa$  in pre-equilibrium phase

# Heavy ion collision in spacetime

## Stages of a heavy ion collision



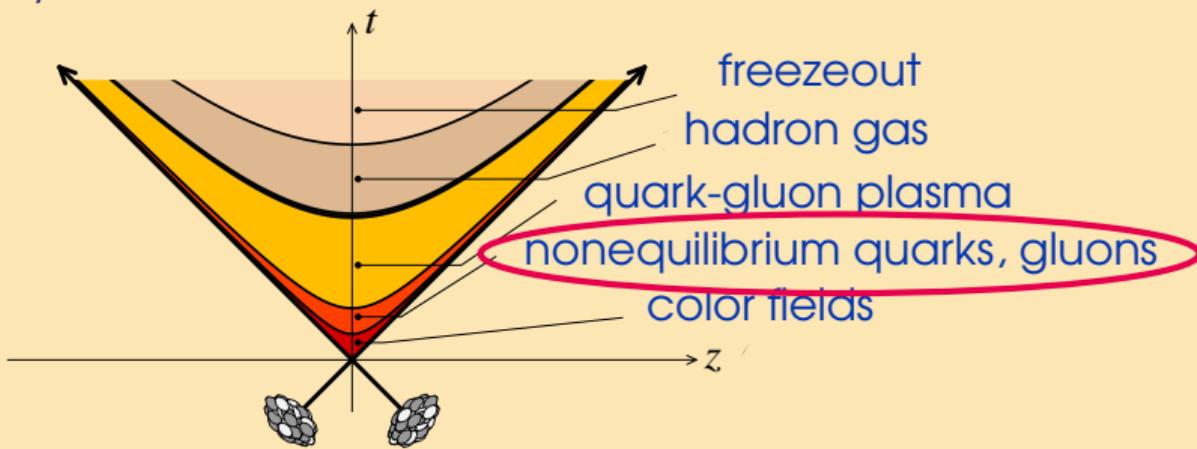
- Timescales for hard  $M \sim m_c, p_T$  probes:

$$1/M \ll 1/Q_s \ll t_{\text{therm}}$$

- Hard probes  $M \sim m_c, p_T$  created first  $\implies$  cannot neglect pre-equilibrium
- Even if thermalization is quick, pre-equilibrium is hot, dense  $\implies$  large effect

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# Transport coefficients pre-equilibrium

$$\left\{ \begin{array}{l} \hat{q} \\ \kappa \end{array} \right\} = \frac{d \langle q_{\perp}^2 \rangle}{dt} \quad \left\{ \begin{array}{l} \text{jet } (p = \infty) \\ \text{H.Q. } (m = \infty) \end{array} \right.$$

- ▶ Standard for a long time:  
 $\hat{q}, \kappa$  in thermal system  
➡ Input for jet quenching, H.Q. diffusion

- ▶ Recent interest: glasma phase

E.g. A. Ipp et al 2001.10001, 2009.14206

Avramescu et al 2303.05599

Carrington et al 2112.06812, 2202.00357, 2304.03241, 2001.05074

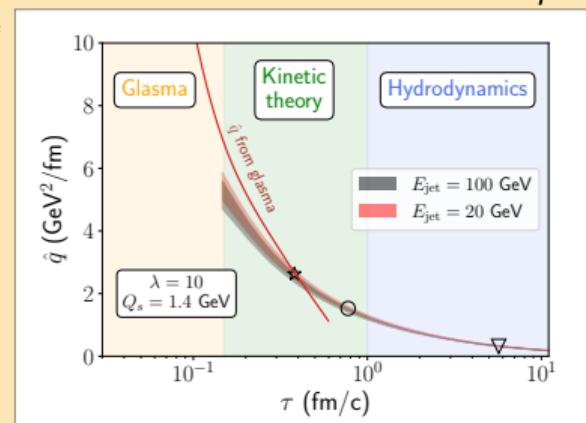
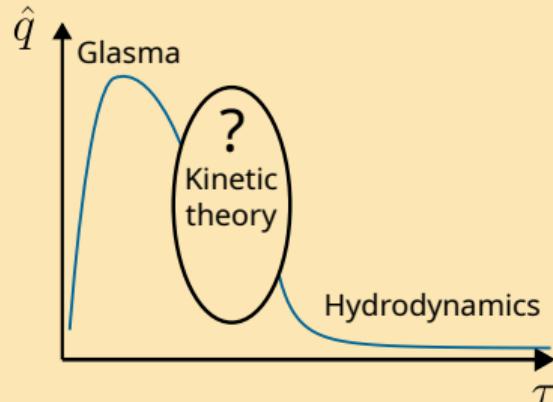
P. Khowal et al 2110.14610

M. Ruggieri et al 2203.06712

Y. Sun et al. 1902.06254

K. Boguslavski et al 2005.02418

- ▶ Aim: complete the picture from the glasma to hydrodynamics



# Bottom-up thermalization

Baier, Mueller, Schiff, Son hep-ph/0009237

3 stages of bottom-up thermalization

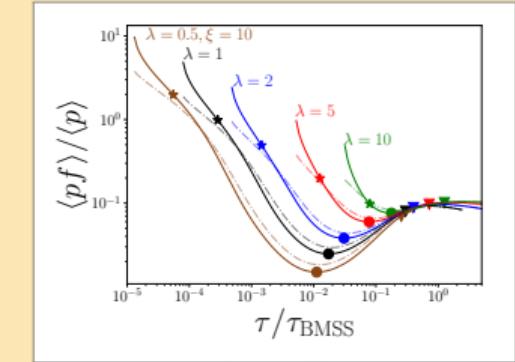
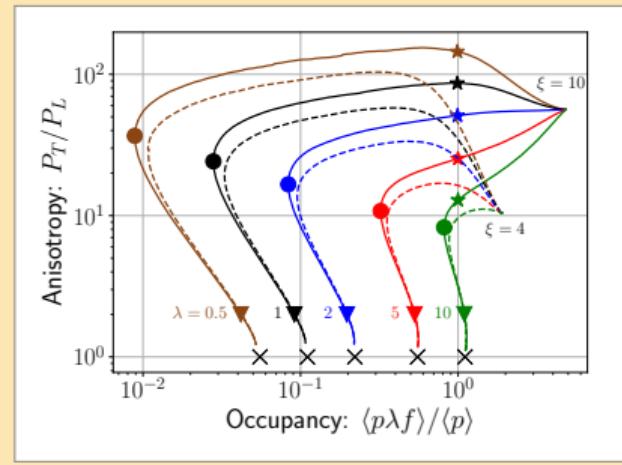
1. Classical field stage ( $0 \rightarrow \star$ ) : growing anisotropy of hard  $\sim Q_s$  modes
2. Bath of soft particles develops ( $\star \rightarrow \bullet$ )
3. Radiative breakup of hard particles ( $\bullet \rightarrow \blacktriangledown$ )

$$\tau_{\text{BMSS}} = \alpha_s^{-13/5} Q_s^{-1}$$

Can be tracked with AMY kinetic theory:

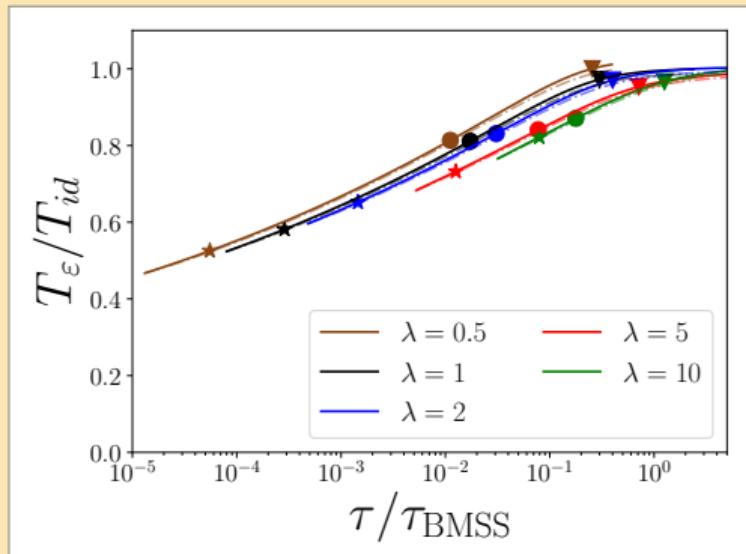
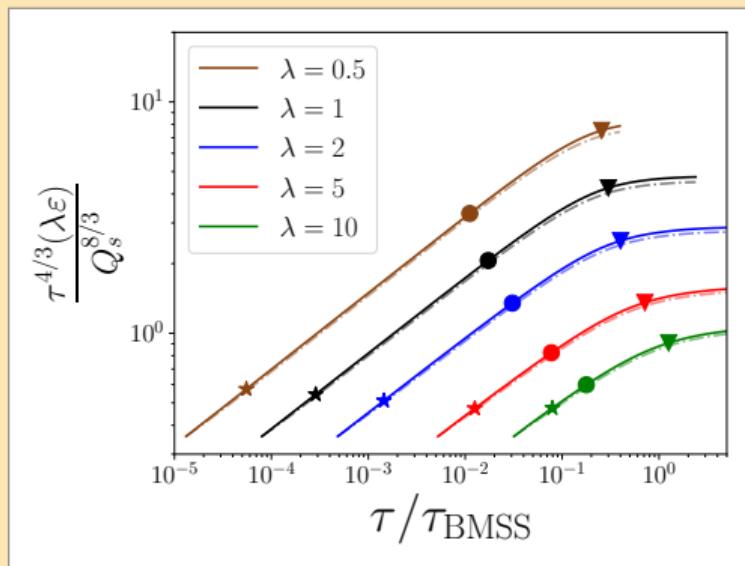
$$-\frac{d}{d\tau} f_{\mathbf{p}} = \mathcal{C}^{2 \leftrightarrow 2}[f_{\mathbf{p}}] + \mathcal{C}^{1 \leftrightarrow 2}[f_{\mathbf{p}}] + \mathcal{C}^{\text{exp}}[f_{\mathbf{p}}].$$

Attractor: different initial conditions converge  
( $\xi$ : initial anisotropy,  $\lambda = 4\pi N_C \alpha_s$ )



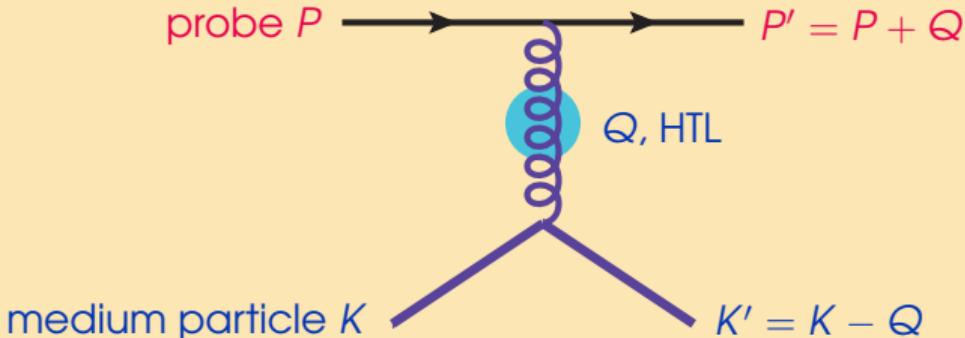
# Convergence to hydro

Most of pre-equilibrium:  $\varepsilon \sim 1/\tau$



$T_{id}$  = bwd extrapolated ideal hydro  
 $T_\varepsilon \sim \sqrt[4]{\varepsilon}$

# Calculating transport coefficients



Momentum broadening from interactions with medium particles:

$$\frac{\hat{q}}{\kappa} \sim \int_{\mathbf{k}\mathbf{k}'\mathbf{p}'} \frac{q_T^2}{E_p} (2\pi)^4 \delta^4(P + K - P' - K') |\mathcal{M}|^2 f(\mathbf{k}) (1 + f(\mathbf{k}')) ,$$

- ▶  $\kappa$ : heavy quark  $P = (M, \mathbf{0})$ ,  $M \rightarrow \infty$
- ▶  $\hat{q}$ : energetic jet  $P^2 = 0$ ,  $p \rightarrow \infty$  (need cutoff  $\hat{q} \sim \ln \Lambda_\perp$ )

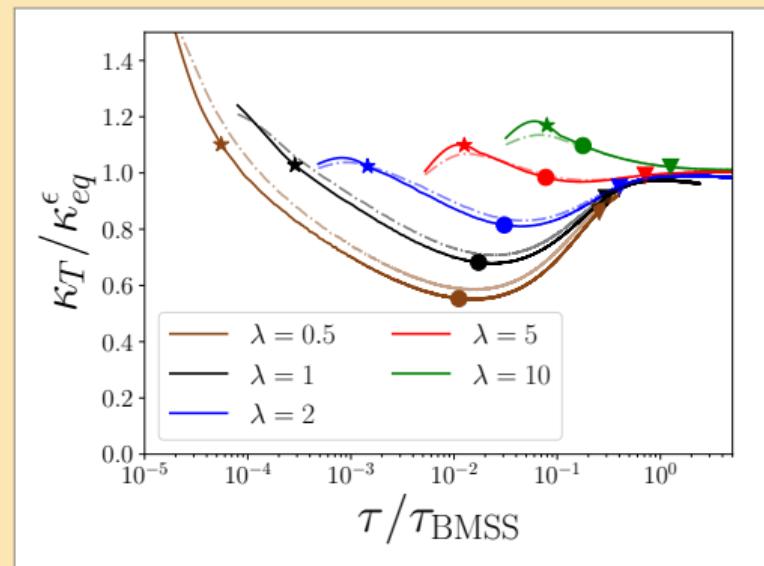
These limits: **medium properties**, not probe

## Result: $\kappa$

Compare to thermal system with same  $\varepsilon$   
(Landau matching,

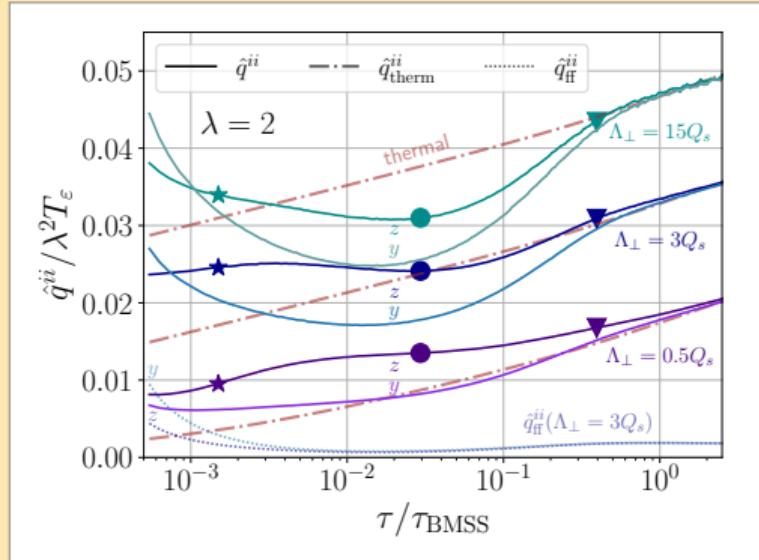
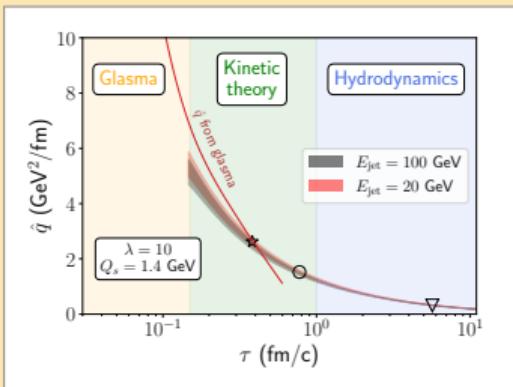
thermal with same  $m_D$  or  $T_*$  is much further)

- ▶ Enhancement first (overoccupied)
  - ▶ Then suppression (underoccupied)
  - ▶ Larger  $\lambda = 4\pi N_c \alpha_s$ :  
behavior smoothed out



Result:  $\hat{q}$

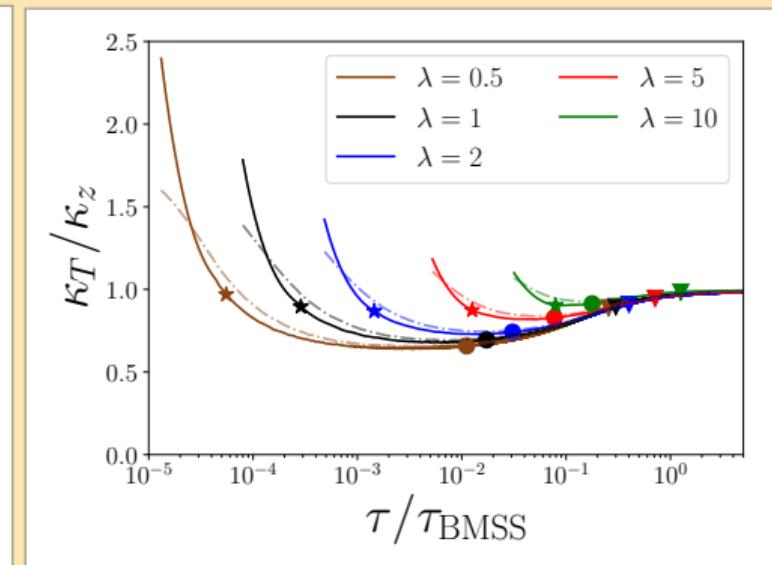
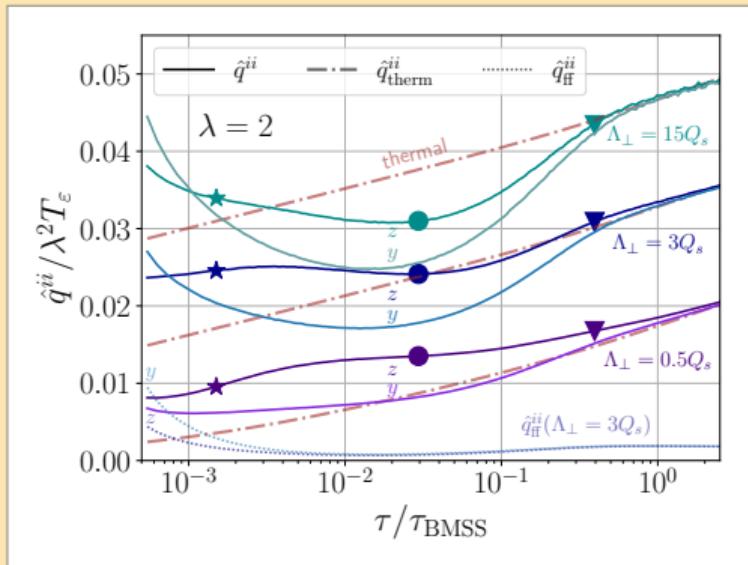
- ▶ Large cutoff  $\Lambda_{\perp}$ :  
Enhancement first, then suppression
  - ▶ Smaller  $\Lambda_{\perp}$ :  
smoother, overall enhancement



- ▶  $\varepsilon \sim 1/\tau$  large
  - ▶ At  $\hat{q}$  value  $\approx$  JETSCAPE estimate (choose  $\Lambda_\perp$ )

# Anisotropy

- Initial overoccupied:  $\kappa_T > \kappa_L, \hat{q}_T > \hat{q}_L \implies$  Bose enhancement, Glasma
- Then underoccupied  $\kappa_T < \kappa_L, \hat{q}_T < \hat{q}_L \implies$  Anisotropy of  $f$



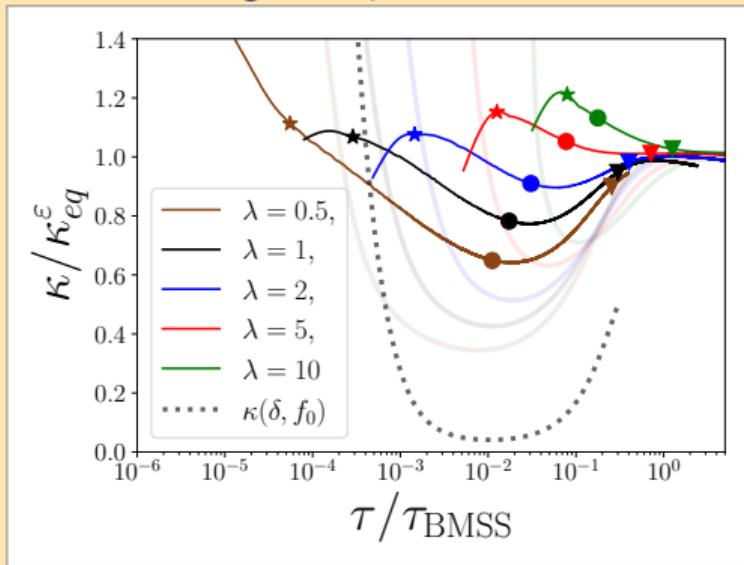
# Relevant microscopic scales

- ▶ Occupation number  $f$
- ▶ Coupling  $\alpha_s$
- ▶ Anisotropy  $\delta \sim \sqrt{\frac{\langle p_z^2 \rangle}{\langle p_T^2 \rangle}}$
- ▶ Hard scale  $p_T^2 \sim Q_s^2$

From these estimate

- ▶ Energy density  $\varepsilon \sim \delta Q_s^4 f$
- ▶ Debye scale  $m_D^2 \sim \alpha_s \delta Q_s^2 f$
- ▶ Soft mode eff. temperature  
 $T_* \sim Q_s(f + 1)$
- ▶  $\kappa \sim m_D^2 T_*$

## Understanding the systematics



(Light:  $T_*$ ,  $m_D$  from EKT, dashed:  $f, \delta$  from EKT)

# Conclusions

- ▶ Pre-equilibrium stage short, but hot  
    ➡ Significant effect on hard observables
- ▶ QCD kinetic theory:  
    trace system from glasma to hydro
  - and calculate transport coefficients
- ▶ First estimate:  $\hat{q}$ ,  $\kappa$  within  $\sim 30\%$  of thermal system **@ same energy density**
  - and pre-equilibrium  $\varepsilon$
- ▶ Qualitative features, anisotropy understood from microscopic quantities  $m_D$ ,  $T_*$

$\hat{q}$  parametrizations available in 2303.12595,  $\kappa$  upon request

